

Robust Control of DC-DC Converter by Approximate 2DOF Digital Controller Realizing First-Order Model

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Abstract: Robust DC-DC converter which can cover extensive load changes and also input voltage changes with one controller is needed. In this paper, we propose a method for determining the parameters of 2DOF digital controller which makes the control bandwidth wider, and at the same time makes a variation of the output voltage very small at sudden changes of resistive load and the input voltage. The 2DOF digital controller whose parameters are determined by the proposed method is actually implemented on a DSP and is connected to a DC-DC converter. Experimental studies demonstrate that this type of digital controller can satisfy given specifications.

Keywords: DC-DC converter, Digital integral-type control system, First-order model, Approximate 2DOF system, Robust control

1. Introduction

In many applications of DC-DC converters, loads cannot be specified in advance, i.e., their amplitudes are suddenly changed from the zero to the maximum rating. Generally, design conditions are changed for each load and then each controller has to be re-designed. Then, a so-called robust DC-DC converter which can cover such extensive load changes and also input voltage changes with one controller is needed. Analog control IC is used usually for the controller of DC-DC converters. Simple integral control etc. are performed with the analog control IC. Moreover, the application of the digital controller to DC-DC converters designed by the PID or root locus method etc. has been considered recently[1], [2]. However it is difficult to retain sufficient robustness of DC-DC converters by these techniques.

The authors proposed the method of designing an approximate 2-degree-of-freedom (2DOF) robust controller of DC-AC converters[3], [4]. For applying this approximate 2DOF controller to DC-DC converters, it is necessary to improve the degree of approximation for better robustness. The authors also proposed the method of designing an approximate 2-degree-of-freedom (2DOF) robust controller of DC-DC converters using a second-order model[5]. In this paper, we propose a new method for designing good approximate 2DOF digital controller using a first-order model which makes the control bandwidth wider, and at the same time makes a variation of the output voltage very small at sudden changes of resistive load. We also show the controller parameter design procedure which performs good approximation. This type of good approximate 2DOF controller is constituted as follows : First, a model matching system with a specified rising time in startup transient response is constituted by using the voltage and the current feedbacks. The current sensor is generally expensive and noisy. In order to avoid use of the current sensor, the current feedback is changed by using a dynamic compensator into the output

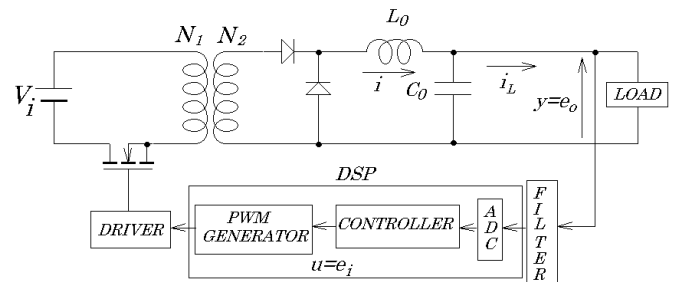


Fig. 1. DC-DC converter

feedback and control input feedback equivalently. Secondly, a first order approximate model of this model matching system is derived. And inverse system of this first order approximate model and a filter for realizing the inverse system are combined with the model matching system. Finally, an equivalent conversion of the portion of the controller is carried out, and a realizable approximate 2DOF controller is obtained. This digital controller is actually realized by using a DSP. Some simulations and experiments show that the proposed high-order approximate 2DOF digital controller can satisfy given specifications.

2. DC-DC converter

The DC-DC converter as shown in Fig.1 has been manufactured. In order to realize the approximate 2DOF digital controller which satisfies given specifications, we use *TITMS320LF* 2401 as DSP. This DSP has a built-in AD converter and a PWM switching signal generating part. The triangular wave carrier is adopted as a PWM switching signal generating part. The switching frequency is set at 300[KHz] and the peak-to-peak amplitude C_m is 66[V]. The LC circuit is a filter for removing carrier and switching noises. L_0 is 1.4[μH], and C_0 is 308[μF]. If the frequency of control input u is smaller enough than that of the carrier, the state equation of the DC-DC converter at resistive load in Fig.1 ex-

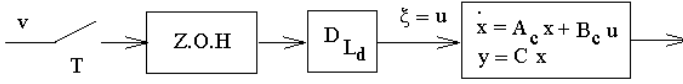


Fig. 2. Controlled object with input dead time $L_d (\leq T)$

cept DSP can be expressed from the state equalizing method (Fukuda and Nakaoka, 1993) as follows:

$$\begin{cases} \dot{x} = A_c x + B_c u \\ y = C x \end{cases} \quad (1)$$

where

$$x = \begin{bmatrix} e_o \\ i \end{bmatrix} \quad A_c = \begin{bmatrix} -\frac{1}{C_0 R_L} & \frac{1}{C_0} \\ -\frac{1}{L_0} & -\frac{R_0}{L_0} \end{bmatrix} \quad B_c = \begin{bmatrix} 0 \\ \frac{K_p}{L_0} \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 0 \end{bmatrix} \quad u = e_i \quad y = e_o \quad K_p = -\frac{V_i N_2}{C_m N_1}$$

When realizing a digital controller by a DSP, a delay time exists between the start point of sampling operation and the output point of control input due to the input computing time and AD/DA conversion times. This delay time is considered to be equivalent to the input dead time which exists in the controlled object as shown in **Fig.2**.

Then the state equation of the system of Fig.2 is expressed as follows:

$$\begin{cases} x_{dw}(k+1) = A_{dw} x_{dw}(k) + B_{dw} v(k) \\ y(k) = C_{dw} x_{dw}(k) \end{cases} \quad (2)$$

where

$$x_{dw}(k) = \begin{bmatrix} x_d(k) \\ \xi_2(k) \end{bmatrix} \quad x_d(k) = \begin{bmatrix} x(k) \\ \xi_1(k) \end{bmatrix}$$

$$A_{dw} = \begin{bmatrix} A_d & B_d \\ 0 & 0 \end{bmatrix} \quad B_{dw} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$A_d = \begin{bmatrix} e^{A_c T} & e^{A_c(T-L_d)} \int_0^{L_d} e^{A_c \tau} B_c d\tau \\ 0 & 0 \end{bmatrix}$$

$$B_d = \begin{bmatrix} \int_0^{T-L_d} e^{A_c \tau} B_c d\tau \\ 1 \end{bmatrix}$$

$$C_{dw} = \begin{bmatrix} C_d & 0 \end{bmatrix} \quad C_d = \begin{bmatrix} C & 0 \end{bmatrix} \quad \xi_1(k) = u(k)$$

In practical use of DC-DC converter, the characteristics of a startup transient response and a dynamic load response are important. The DC-DC converter with the following specifications (1)-(6) is designed and manufactured by constituting digital controller to DC-DC switching part.

1. Input voltage V_i is 48[V] and output voltage e_o is 3.3[V].
2. Startup transient responses are almost the same at resistive load and parallel load of resistance and capacity, where $0.165 \leq R_L < \infty [\Omega]$, $0 \leq C_L \leq 200 [\mu F]$.
3. The rising time in startup transient response is smaller than 100[μs].
4. Against all the loads of spec.2, an over-shoot is not allowable in startup transient response.

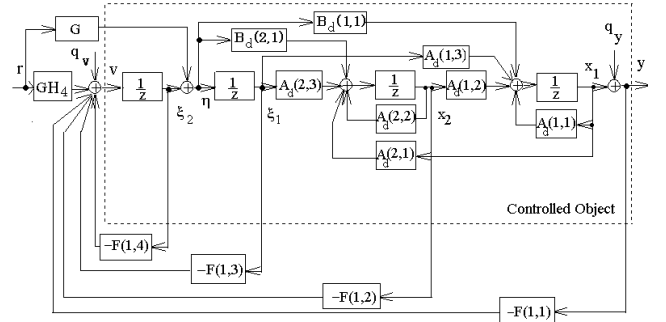


Fig. 3. Equivalent disturbances due to load variations (parameter variations) and model matching system with state feedback

5. The dynamic load response is smaller than 50[mV] against 10[A] change of load current.
6. The specs. (2),(3),(4) and (5) are satisfied also to change of input voltage of $\pm 20\%$.

The load changes for the controlled object and the input voltage change are considered as parameter changes in eq.(2). Such parameter changes can be transformed to equivalent disturbances q_v and q_y as shown in **Fig.3** even in discrete-time systems. Moreover, if the saturation in the input arises or the input frequency is not so small as the carrier frequency, the controlled object will be regarded as a class of nonlinear systems. Such characteristics changes can be also transformed to equivalent disturbances as shown in Fig.3. Therefore, what is necessary is just to constitute the control systems whose pulse transfer functions from equivalent disturbances q_v and q_y to the output y become as small as possible in their amplitudes, in order to robustize or suppress the influence of these parameter changes, i.e., load changes, and input voltage change. In the next section, an easily designing method which makes it possible to suppress the influence of such disturbances with the target characteristics held will be presented.

3. Design of good approximate 2DOF digital integral-type control system

First, the transfer function between the reference input r and the output y is specified as follows:

$$W_{ry} =$$

$$\frac{(1+H_1)(1+H_2)(1+H_3)(z-n_1)(z-n_2)(z+H_4)}{(1-n_1)(1-n_2)(z+H_1)(z+H_2)(z+H_3)(z+H_4)} \quad (3)$$

where, n_1 and n_2 are the zeros for discrete-time control object (2). It shall be specified that the relation of H_1 and H_2 , H_3 becomes $|H_1| \gg |H_2|$ and $|H_3|$. Then $W_{ry}(z)$ can be approximated in the following manner:

$$W_{ry}(z) \approx W_m(z) = \frac{1+H_1}{z+H_1} \quad (4)$$

This target characteristic $W_{ry}(z) \approx W_m(z)$ is specified to satisfy the specs.(3) and (4).

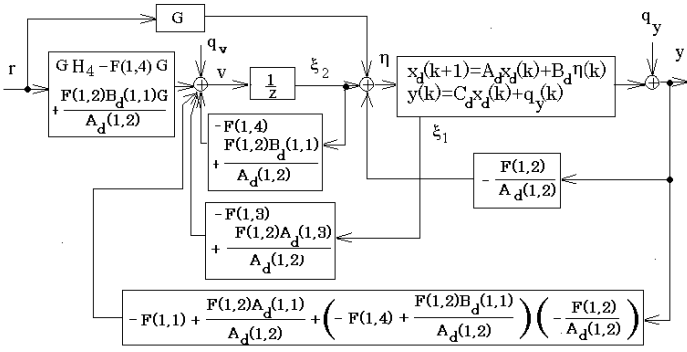


Fig. 4. Model matching system using only voltage (output) feedback

Applying a state feedback

$$\begin{aligned} v &= -Fx^* + GH_4 r \\ x^* &= [y \ x_2 \ \xi_1 \ \xi_2]^T \end{aligned} \quad (5)$$

and feedforward

$$\xi_1(k+1) = Gr \quad (6)$$

to the discrete-time controlled object as shown in Fig.3, we decide $F = [F(1,1) \ F(1,2) \ F(1,3) \ F(1,4)]$ and G so that $W_{ry}(z)$ becomes eq.(3). The current feedback is used in Fig.3. This is transformed to voltage and control input feedbacks, without changing the pulse transfer function between $r-y$ by an equivalent conversion. The following relation is obtained from Fig.3:

$$\begin{aligned} -F(1,2)x_2(k) &= -\frac{F(1,2)}{A_d(1,2)}(x_1(k+1) \\ -A_d(1,1)x_1(k) &- A_d(1,3)\xi_1 - B_d(1,1)\eta) \end{aligned} \quad (7)$$

If the current feedback is transformed equivalently using the right-hand side of this equation, the control system with only voltage feedback as shown in **Fig.4** will be obtained. The transfer function $W_{Qy}(z)$ between this equivalent disturbance $Q = [q_v \ q_y]^T$ and y of the system in Fig.4 is defined as

$$W_{Qy}(z) = [W_{q_v y}(z) \ W_{q_y y}(z)] \quad (8)$$

The system added the inverse system and filter to the system in Fig.4 is constituted as shown in **Fig.5**. In Fig.5, the transfer function $F(z)$ becomes

$$F(z) = \frac{k_z}{z-1+k_z} \quad (9)$$

The transfer functions between $r-y$ and $Q-y$ of the system in Fig.5 are given by

$$y = \frac{(1+H_1)}{(z+H_1)} \frac{z-1+k_z}{z-1+k_z W_s(z)} W_s(z) r \quad (10)$$

$$y = \frac{z-1}{z-1+k_z} \frac{z-1+k_z}{z-1+k_z W_s(z)} W_{Qy}(z) Q \quad (11)$$

where

$$W_s(z) = \frac{(1+H_2)(1+H_3)(z-n_1)(z-n_2)}{(z+H_2)(z+H_3)(1-n_1)(1-n_2)} \quad (12)$$

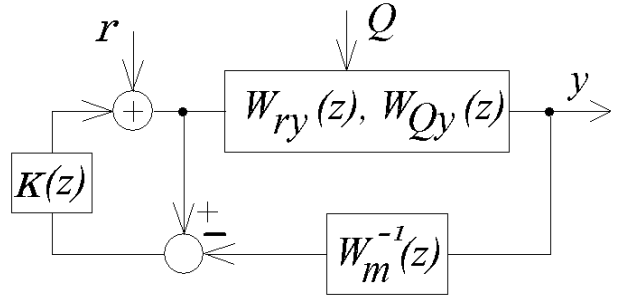


Fig. 5. System reconstituted with an inverse system and a filter

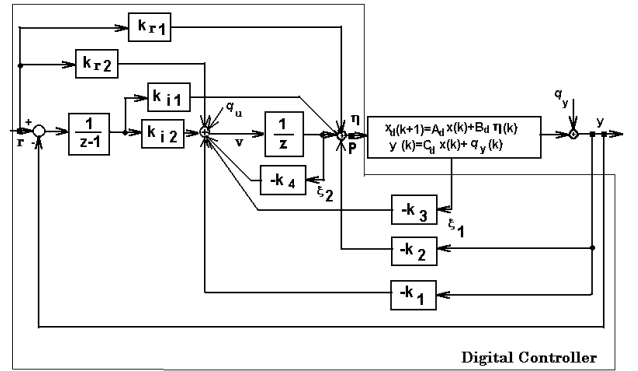


Fig. 6. Approximate 2DOF digital integral-type control system

Here, if $W_s(z) \approx 1$, then eqs.(10) and (11) become, respectively,

$$y \approx \frac{1+H_1}{z+H_1} r \quad (13)$$

$$y \approx \frac{z-1}{z-1+k_z} W_{Qy}(z) Q \quad (14)$$

From eqs.(13) and (14), it turns out that the characteristics from r to y can be specified with H_1 , and the characteristics from Q to y can be independently specified with k_z . That is, the system in Fig.5 is an approximate 2DOF system, and its sensitivity against disturbances, i.e., load change becomes lower with the increase of k_z .

If an equivalent conversion of the controller in Fig.5 is carried out, the approximate 2DOF digital integral-type control systems will be obtained as shown in **Fig.6**. In Fig.6, the parameters of the controller are as follows:

$$\begin{aligned} k_1 &= F(1,1 + F(1,2)FF(1,1) + (-F(1,4) \\ &- F(1,2)FF(1,4))(-F(1,2)/FF(1,2))) \\ &+ (GH_4 + GF_z)(k_z/(1+H_2)) \\ k_2 &= F(1,2)/FF(1,2) + G(k_z/(1+H_2)) \\ k_3 &= F(1,3) + F(1,2)(FF(1,3)) \quad k_4 = -F_z \\ k_{i1} &= Gk_z \quad k_{i2} = (GH_4 + GF_z)k_z \\ k_{r1} &= G \quad k_{r2} = GH_4 + GF_z \end{aligned} \quad (15)$$

where

$$FF(1,1) = -A_d(1,1)/A_d(1,2)$$

$$\begin{aligned}
FF(1,2) &= A_d(1,2) \\
FF(1,3) &= -A_d(1,3)/A_d(1,2) \\
FF(1,4) &= -B_d(1,1)/A_d(1,2) \\
F_z &= -F(1,4) - F(1,2)FF(1,4)
\end{aligned}$$

Now, for good approximation, i.e., in order to let eqs.(10) and (11) approach further to the right-hand side of eqs.(13) and (14) respectively, what is necessary is just to set up so that $W_s(z)$ may approach to 1 further in the large frequency range. Moreover, it is necessary to make the gain of eq.(14) small for low sensitivity. For the purpose, while the gain of W_{Qy} is made small, we have to make k_z into large value. However, if k_z is enlarged, the roots of following equation in eq.(10) may approach H_1 , and the degree of approximation may become not so good.

$$z - 1 + k_z W_s(z) = 0 \quad (16)$$

The roots of eq.(16) are ones of whole systems except for H_1 and H_4 . When k_z is made to increase from 0, these roots leave 1, $-H_2$, and $-H_3$, and when k_z is set as a certain value, they become certain values like p_1 , p_2 , and p_3 . If we determine $-H_2$ and $-H_3$ so that the following equation is satisfied and the absolute value of the real number part of those become small suitably when k_z is sufficiently large value, the degree of approximation of eqs.(10) and (11) will become good, and low sensitivity will also become good.

$$(|Re(p_1)|, |Re(p_2)|, |p_3|) \ll |H_1| \quad (17)$$

If p_1 , p_2 , and p_3 are specified like eq.(17) and k_z is specified to be a suitable value, we can search for starting point H_2 and H_3 of root loci, reversely. If the roots of eq.(16) are specified to be p_1 , p_2 , and p_3 , the following equation will be obtained from eq.(12).

$$\begin{aligned}
(1 - n_1)(1 - n_2)(z - 1)(z + H_2)(z + H_3) \\
+ k_z(1 + H_2)(1 + H_3)(z - n_1)(z - n_2) \\
= (z - p_1)(z - p_2)(z - p_3)
\end{aligned} \quad (18)$$

Substituting $H_2 = x + yi$, $H_3 = x - yi$, and the value of k_z for eq.(18), and setting the coefficient of each power of z equally, the equation of three circles about x and y will be obtained. H_2 and H_3 can be determined from the intersection of these circles. The design procedure of the parameters of the controller is shown as follows:

1. H_1 is set up so that the specified rising time is satisfied.
2. H_4 is set up as

$$|H_4| \approx 0.5|H_1| \quad (19)$$

3. The roots of eq.(16) are set up as

$$\begin{aligned}
p_1 &\approx -0.5H_1 + 0.5H_1i & p_2 &\approx -0.5H_1 - 0.5H_1i \\
p_3 &\approx -0.5H_1
\end{aligned} \quad (20)$$

4. k_z of eq.(16) are set up as

$$k_z \approx 0.5 \quad (21)$$

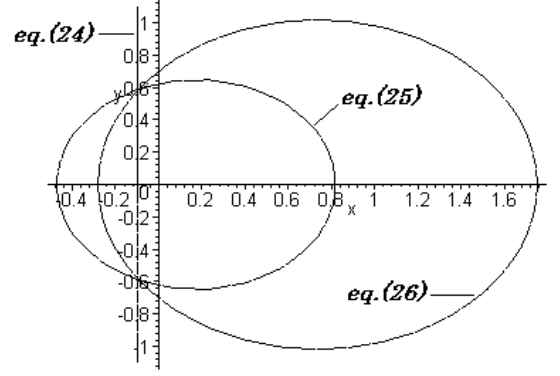


Fig. 7. Circles of eqs.(27),(28) and (29)

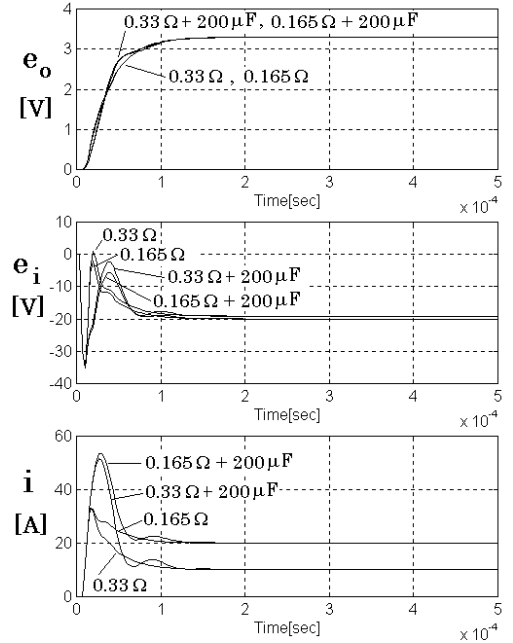


Fig. 8. Simulation results of startup responses at various loads

5. Determine H_2 and H_3 so that the roots of eq.(16) become equal to p_1 , p_2 and p_3 .
6. Determine the parameters of the controller from eq.(15).
7. Check whether all the specifications are satisfied by simulation.
8. When not satisfying the specification, 4. is changed a little and the next 5. are repeated.
9. Furthermore when not satisfying the specification, 3. is changed a little and the next 4. are repeated.

4. Experimental studies

The sampling period T are set as $3.3[\mu s]$ and the input dead time L_d is about $0.999T[\mu s]$. We will design a control system so that all the specifications are satisfied. First of all, in order to satisfy the specification on the rising time in startup transient response, from design procedures 1. and 2., H_1 , and

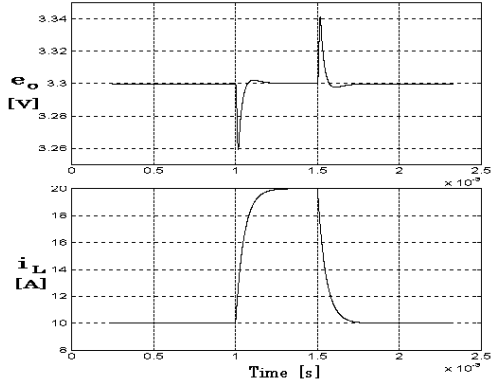


Fig. 9. Simulation result of dynamic load response at resistive load

H_4 are set as

$$H_1 = -0.89 \quad H_4 = -0.3 \quad (22)$$

In order to increase the degree of the approximation in eqs.(13) and (14) over the large frequency range, what is necessary is just to make the absolute value of the real part of the roots of eq.(16) as small as possible. Substituting

$$H_2 = x + yi \quad H_3 = x - yi \quad (23)$$

into eq.(18), we get

$$\begin{aligned} & (k_z x^2 + (2k_z - 2n_2 + 2n_1 n_2 - 2n_1 + 2)x \\ & + k_z y^2 + (-1 + n_2 + k_z - n_1 n_2 + n_1))/(1 - n_2 - n_1 \\ & + n_1 n_2) = -p_1 - p_3 - p_2 \end{aligned} \quad (24)$$

$$\begin{aligned} & (-k_z n_1 + n_1 n_2 - n_2 + 1 - n_1 - k_z n_2)x^2 \\ & + (2n_2 + 2n_1 - 2k_z n_2 - 2n_1 n_2 - 2k_z n_1 - 2)x \\ & + (-k_z n_1 + n_1 n_2 - n_2 + 1 - n_1 - k_z n_2)y^2 \\ & - k_z n_2 - k_z n_1)/(1 - n_2 - n_1 + n_1 n_2) \\ & = p_1 p_3 + p_1 p_2 + p_2 p_3 \end{aligned} \quad (25)$$

$$\begin{aligned} & (-1 + n_2 + k_z n_1 n_2 - n_1 n_2 + n_1)x^2 \\ & + 2k_z n_1 n_2 x + (-1 + n_2 + k_z n_1 n_2 \\ & - n_1 n_2 + n_1)y^2 + k_z n_1 n_2)(1 - n_2 - n_1 \\ & + n_1 n_2) = -p_1 p_2 p_3 \end{aligned} \quad (26)$$

These are circle equations when fixing k_z . From procedures 3. and 4., setting as

$$\begin{aligned} p_1 &= 0.35 + 0.5i \quad p_2 = 0.35 - 0.5i \quad p_3 = 0.5 \\ k_z &= 0.3 \quad n_1 = -0.97351 \quad n_2 = -0.97731e6 \end{aligned} \quad (27)$$

and substituting these into eqs.(24),(25) and (26), we get

$$2x + 0.0000016x^2 + 0.0000016y^2 + 0.2 = 0 \quad (28)$$

$$-1.696x + 1.152x^2 + 1.152y^2 - 0.570 = 0 \quad (29)$$

$$0.296x - 0.852x^2 - 0.852y^2 + 0.334 = 0 \quad (30)$$

These circles are drawn in Fig.7. From the intersect point, we get

$$x = -0.1 \quad y = 0.6 \quad (31)$$

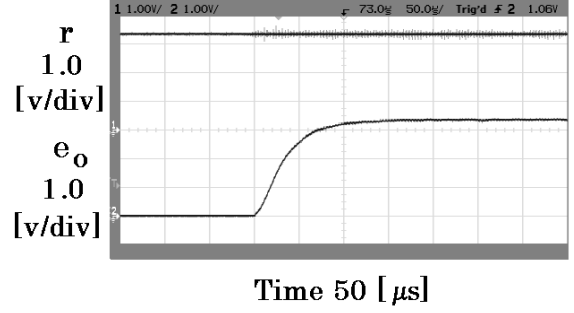


Fig. 10. Experimental startup response at $R_L = 0.33[\Omega]$

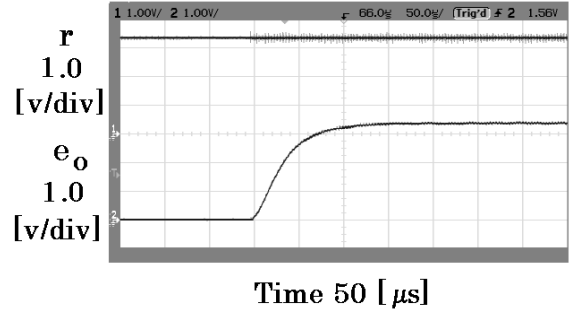


Fig. 11. Experimental startup response at $R_L = 0.165[\Omega]$

Then, from the procedure 6., the parameters of controller become

$$\begin{aligned} k_1 &= -332.223 \quad k_2 = 260.57 \quad k_3 = -0.51638 \\ k_4 &= -0.51781 \quad k_i = 7.0594 \quad k_{iz} = -8.6321 \end{aligned} \quad (32)$$

It must be better that k_{r1} and k_{r2} are set to 0, since the characteristics of the control system hardly changes in this case.

The simulation results of the startup responses are shown in Fig.8. From the output voltage $y = e_o$ in this figure, it turns out that the specifications are satisfied. It is checked that almost the same simulation results as Fig.8 are obtained when the input voltage V_i is changed by $\pm 20\%$. The simulation result of the dynamic load responses is shown in Fig.9. Fig.9 is the result at resistive load and the value is changed as $R_L = 0.33 \leftrightarrow 0.165[\Omega]$. It is checked that almost the same simulation result as Fig.9 is obtained at parallel load of resistance ($R_L = 0.33 \leftrightarrow 0.165[\Omega]$) and capacity ($C_L = 200[\mu F]$). It turns out that all the specifications are satisfied.

Experimental results when realizing the digital controller with the parameters of eq.(32) by using the DSP, and connecting to the controlled object of eq.(1) are shown in Figs.10-15. Fig.10 and Fig.11 show startup responses at resistive loads $R_L = 0.33[\Omega]$ and $R_L = 0.165[\Omega]$, respectively. Fig.12 shows a startup response at parallel load of resistance $R_L = 0.33[\Omega]$ and capacity $C_L = 200[\mu F]$. Fig.13 shows a startup response at parallel load of resistance $R_L = 0.165[\Omega]$ and capacity $C_L = 200[\mu F]$. From $y = e_o$ in these figure, it turns out that almost the same experimental results as the simulation ones in Fig.8 are obtained and the specifications

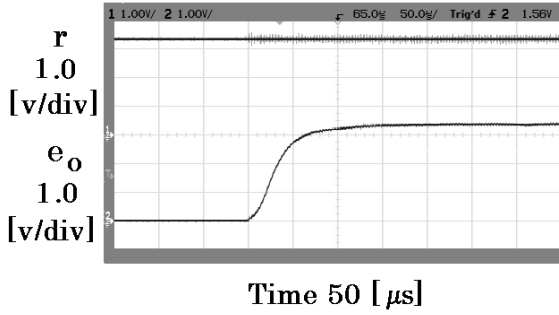


Fig. 12. Experimental startup response at parallel load of $R_L = 0.33[\Omega]$ and $C_L = 200[\mu\text{F}]$

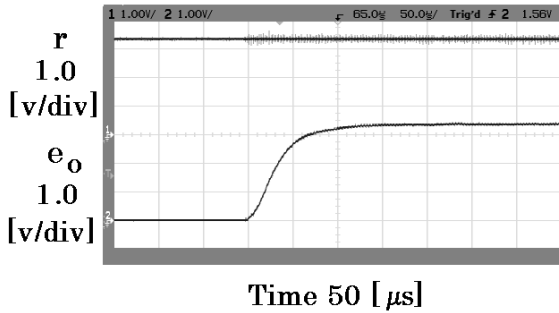


Fig. 13. Experimental startup response at parallel load of $R_L = 0.165[\Omega]$ and $C_L = 200[\mu\text{F}]$

are satisfied. Fig.14 shows a startup response at resistive load $R_L = 0.33[\Omega]$ when the input voltages are 58[V]. It is checked that almost the same experimental result is obtained at resistive load $R_L = 0.33[\Omega]$ when the input voltage is 38[V]. It turns out that the specifications are satisfied when the input voltage V_i is changed by $\pm 20\%$. Fig.15 shows a dynamic load response at resistive load and the value changed as $R_L = 0.33 \leftrightarrow 0.165[\Omega]$. It turns out that almost the same experimental results as the simulation results in Fig.9 are obtained. It is checked that almost the same experimental results as Fig.15 are obtained at the parallel load of resistance ($R_L = 0.33 \leftrightarrow 0.165[\Omega]$) and capacity ($C_L = 200[\mu\text{F}]$). Although load current (i_L) changed suddenly from 20 [A] to 10 [A] or reverse, output voltage change is very small and is suppressed within about 50[mV]. It turns out that all the specifications are satisfied.

5. Conclusion

In this paper, the concept for controller of DC-DC converter to attain the good robustness against an extensive load changes and input voltage change was given. The proposed digital controller was implemented on the DSP connecting to the controlled object. It was shown from some simulations and experiments that a sufficiently robust digital controller is realizable. The characteristics of the startup transient response and the dynamic load response were improved by using the proposed good approximate 2DOF digital controller. A control algorithm has been implemented with a short sampling time using DSP. This fact demonstrates the usefulness and practicality of our method. The future work is experi-

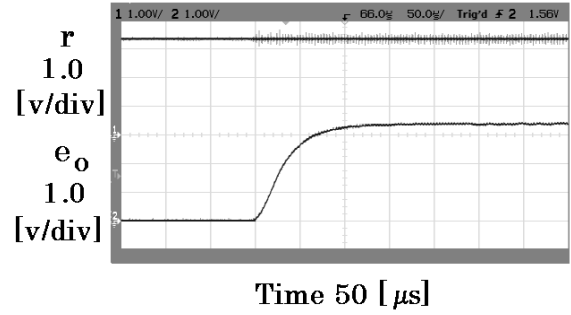


Fig. 14. Experimental result of a startup response at resistive load ($R_L = 0.33[\Omega]$) when the input voltage is 58[V]

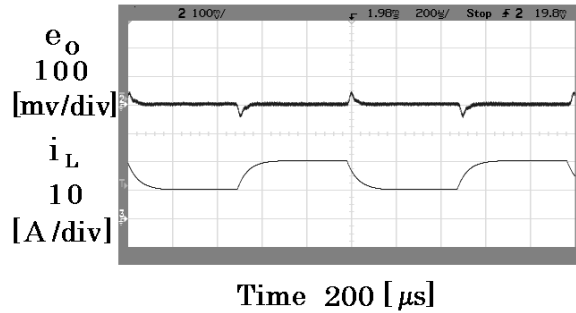


Fig. 15. Experimental dynamic load response at $R_L = 0.33 \leftrightarrow 0.165[\Omega]$

mental studies on a sudden change of the input voltage.

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